

## Cost of Capital

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João Carvalho das Neves  
Professor of Corporate Finance & Real Estate Finance  
ISEG, Universidade de Lisboa  
jcneves@iseg.ulisboa.pt

### Types of cost of capital that you need to address

- Cost of equity ( $k_e$ )
- Cost of debt ( $k_d$ )
- Cost of preferred capital ( $k_p$ )
- WACC ( $k_m$ )
- Unlevered cost of capital ( $k_u$ )



## i. Cost of equity (ke)

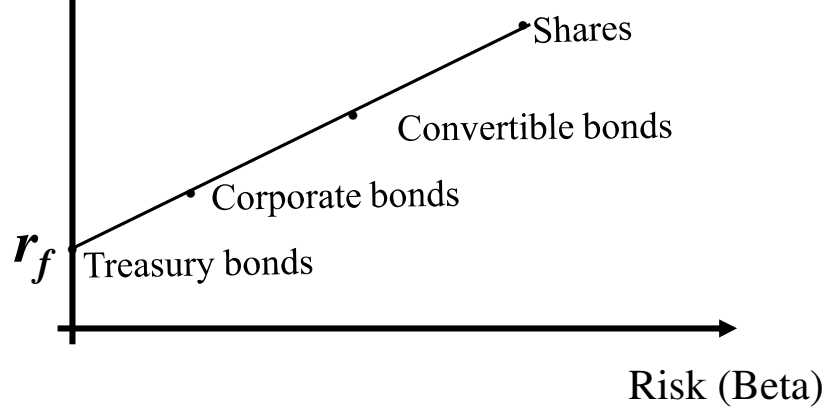
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## Financial markets (CAPM - Capital Asset Pricing Model)

Return

$$k_e = r_f + \beta \cdot (r_m - r_f)$$



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## Models to estimate the cost of equity

- Historical based
  - CAPM
  - CAPM 2º moment
  - D-CAPM
  - Merton
  - APM - Arbitrage Pricing Model
  - Multifactors (Fama e French)
  - Regression
- Accounting Approach
  - Modigliani e Miller
  - Covariance of operational income
  - Covariance of sales
- Implicit prices using options models
  - Shares (Hsia)
  - Options on shares (McNulty)
- Implicit prices using discounting models
  - Models of Gordon, Malkiel, H
  - EVA Model
  - DCF
- Compound betas
  - Leverage effect
  - Conservation of risk
  - Simultaneous equations
  - Regression of Business Units

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## Most commonly used models to estimate the cost of equity (ke)

\* CAPM

$$k_e = r_f + \beta(r_m - r_f)$$

$r_f$  = Risk free rate of return  
 $\beta$  = Beta  
 $r_m$  = Market return  
 $r_m - r_f$  = Market risk premium

\* THE GORDON MODEL

$$k_e = \frac{d_1}{P_0} + g$$

$d_1$  = Dividend per share year 1  
 $P_0$  = Share price year 0  
 $g$  = Growth rate in the long term

\* THE MODIGLIANI & MILLER (M&M) MODEL

$$k_e = k_u + (k_u - k_d) \times \frac{D}{E} \times (1-t)$$

$k_u$  - Unlevered cost of capital  
 $D$  - Debt  
 $E$  - Equity  
 $t$  - Corporate income tax rate

\* INTUITIVE MODELS

$$k_e = k_d + \rho$$

$$k_e = r_f + \eta$$

$k_d$  = Cost of debt  
 $\rho$  = Risk premium over debt  
 $\eta$  = Risk premium over Treasury Bonds

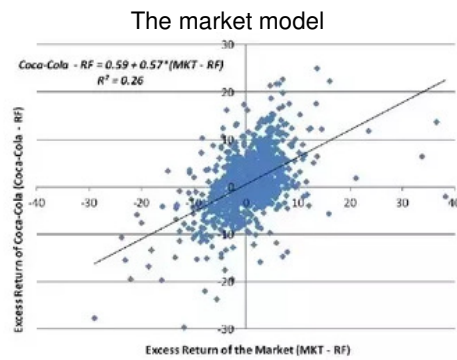
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## CAPM - A standard in the market

$$r_e = r_f + \beta(r_m - r_f)$$

$$r_e - r_f = \alpha + \beta(r_m - r_f)$$

CAPM  
The market model



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## Choosing the CAPM variables!

- Risk free rate
  - Which rate to choose?
  - Stationary or variable?
- Market risk premium
  - Stationary or variable?
- Betas
  - Raw data, adjusted for market conditions, adjusted for trends?
- Cost of equity
  - Stationary or variable?
  - Nominal terms or real terms (constant)?

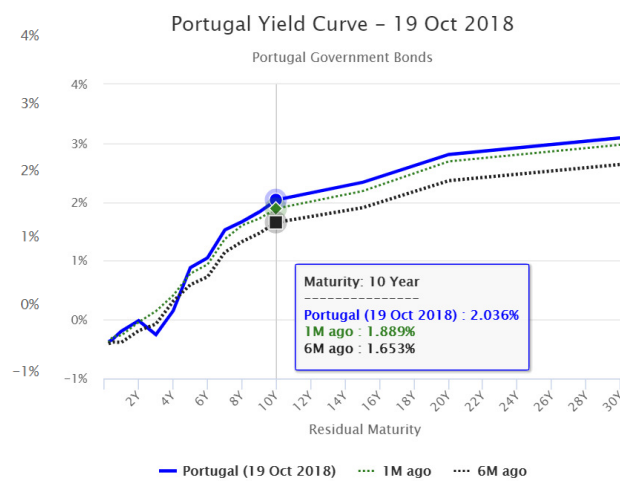
$$r_e = r_f + \beta \cdot (r_m - r_f)$$

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## Risk free rate



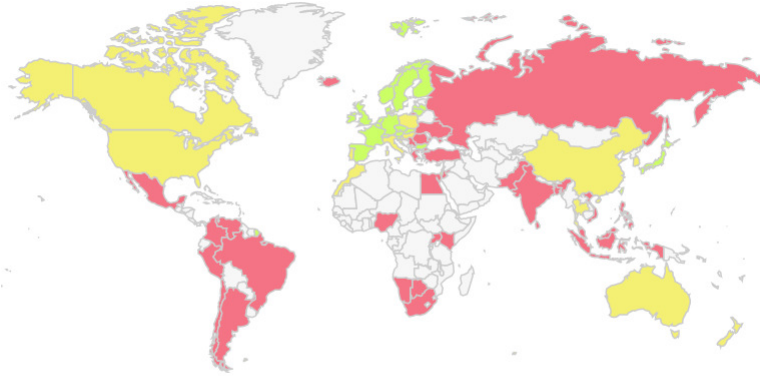
## Yield Curve (Treasury Bonds Portuguese Government)



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Source: <http://www.worldgovernmentbonds.com/country/portugal/>

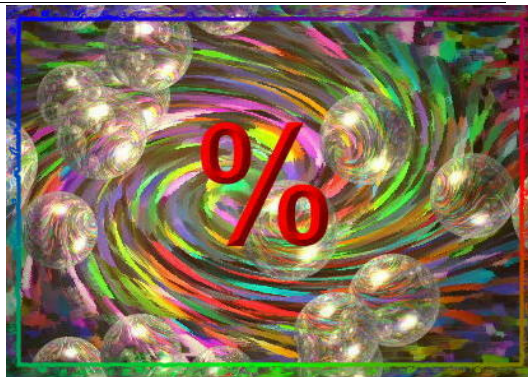
## 10 Y Bond Yield around the world



<http://www.worldgovernmentbonds.com/>

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## Market risk premium ( $R_m - R_f$ )



## Three ways to estimate risk premium

- Investor's Survey - inquiry investors on required risk premiums and use the average premium from these surveys.
- Historical (naïve) risk premium - Assume that the risk premium delivered over long-term periods is equal to the expected premium.
- Implied risk premium - in today's asset prices.

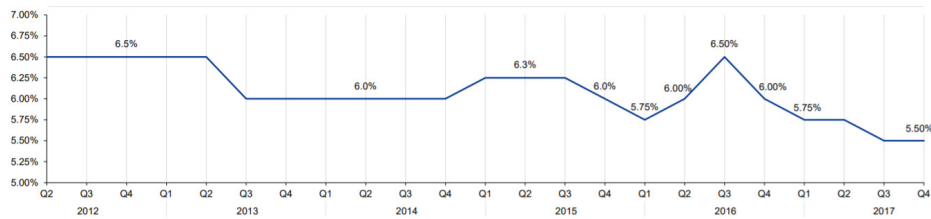
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## 1. Investor's Surveys

- Impractical surveying all investors in a market place.
- Surveys are usual sent to a sample of few individuals and use these results. Examples:
  - Investors Securities Industries Association (individual investors);
  - Merrill Lynch (Institutional Investors);
  - Campbell Harvey & Graham (CFOs);
  - Pablo Fernandez (Analysts) and (Academics)
- The limitations of this approach are:
  - There are no constraints on reasonability
  - The survey results are backward looking
  - They tend to be short term; even the longest surveys do not go beyond one year

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## 2. Historical (naïve) equity risk premium is non-stationary



Source: KPMG, Nederlands, Equity Market Risk Premium – Research Summary, 24 January 2018

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## Standard error of equity risk premium against the number of years

Estimation Period	Standard Error of Risk Premium Estimate
5 years	$20\% / \sqrt{5} = 8.94\%$
10 years	$20\% / \sqrt{10} = 6.32\%$
25 years	$20\% / \sqrt{25} = 4.00\%$
50 years	$20\% / \sqrt{50} = 2.83\%$
80 years	$20\% / \sqrt{80} = 2.23\%$

The longer the series is, the smaller the standard error

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## Can we trust the past?

- Noisy estimates:
  - Even with long time periods of history, the risk premium that you derive will have substantial standard error.
    - If you have 80 years of historical data and you assume a standard deviation of 20% in annual stock returns, the Standard Error in the Risk Premium would be =  $20\% / \sqrt{80} = 2.26\%$
- Survivorship Bias:
  - Using historical data from equity markets creates a sampling bias.

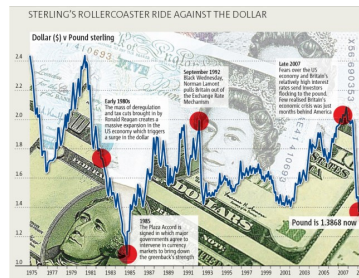
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## 3. Implied risk premium

- If shares are correctly priced in the market and we can estimate the expected cash flows from buying these shares, then we can estimate the expected rate of return by computing the internal rate of return. Subtracting out the risk free rate yields the implied equity risk premium.
- This implied equity premium is a forward looking approach
- It can be updated as often as you want (every minute of every day if you wish).

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## The country risk affects the equity risk premium



## Equity risk premium varies across countries

TABLE 3  
Equity Premium for Selected Countries

Country	Period	Mean real return		
		Market index (%)	Relatively riskless security (%)	Equity premium (%)
United Kingdom	1900–2005	7.4	1.3	6.1
Japan	1900–2005	9.3	–0.5	9.8
Germany	1900–2005	8.2	–0.9	9.1
France	1900–2005	6.1	–3.2	9.3
Sweden	1900–2005	10.1	2.1	8.0
Australia	1900–2005	9.2	0.7	8.5
India	1991–2004	12.6	1.3	11.3

Source: Dimson et al. (2002) and Mehra (2007) for India.

## Macro determinants of equity risk premium

- Economic risk: If the underlying economy is more uncertain, equity risk will be higher.
  - Higher volatility in the GDP implies higher equity risk.
- Political risk: The higher the uncertainty about fiscal and government policy implies higher level of equity risk.
- Market transparency: If information provided by companies are more transparent, equity risk premiums would be lower.
- Liquidity: Markets with higher level of liquidity would have lower level of equity risk.
- Catastrophic risk: The perceived likelihood to occur catastrophic risk in investing in equities, would increase the equity risk.

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## How to measure country risk: 1 - Sovereign ratings

### Long-term sovereign debt ratings

Outlook: p= positive; s= stable; n= negative;  
CWn= credit watch negative

Country	Ratings Agency			Investment Grade Ratings
	Moody's	S&P	Fitch	
Britain	Aa1 s	AAA s	AAA n	Aaa/AAA Minimal risk
U.S.A.	Aaa n	AA+ n	AAA n	
Japan	Aa3 s	AA- n	A+ n	
<b>Euro zone</b>				
Finland	Aaa s	AAA s	AAA s	Aa/AA Very low
Germany	Aaa n	AAA s	AAA s	
Luxembourg	Aaa n	AAA s	AAA s	A/A Low risk
Netherlands	Aaa n	AAA n	AAA s	
Austria	Aaa n	AA+ s	AAA s	Baa/BBB Moderate risk
France	Aa1 n	AA+ n	AAA n	
Belgium	Aa3 n	AA n	AA s	
Estonia	A1 s	AA- s	A+ s	Ba/BB Substantial risk
Slovakia	A2 s	A s	A+ s	
Malta	A3 s	BBB+ s	A+ s	
Slovenia	Baa2 s	A CWn	A- n	B/B High risk
Italy	Baa2 n	BBB+ n	A- n	
Spain	Baa3 n	BBB- n	BBB n	Caa/CCC Very high
Ireland	Ba1 n	BBB+ n	BBB+ s	
Portugal	Ba3 n	BB n	BB+ n	SD/RD Selective Default Restricted Default
Cyprus	Caa3 n	CCC+ n	B n	
Greece	C s	B- s	CCC s	

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Sources: Moody's, Standard & Poor's, Fitch

Staff: 24/02/2013

BEUTERS

## How to measure country risk: 2 - Country Risk Scores (0 a 100)

- The PRS Group
  - Political Risk Services
- ICRG
  - International Country Risk Guide
- The Economist

**Economist.com rankings**

**Country risk**  
Selected countries and territories, July 2008 (except where noted)

Least risky		Most risky	
Rank	Score*	Rank	Score
1	Switzerland †	120	Zimbabwe
2	Finland	119	Iraq
	Norway	118	Sudan
	Sweden **	117	Myanmar
5	Austria ††	116	Jamaica
6	Canada	115	Nicaragua
	Denmark †	114	Cuba
8	Germany **		Kenya
	Netherlands §	112	Cambodia
10	France **		Ecuador
11	Belgium **	110	Vietnam
	Singapore	109	Côte d'Ivoire
13	Hong Kong		Syria
	Japan	107	Lebanon
	Britain #		Venezuela

\*Out of 100, with higher numbers indicating more risk. Scores are based on indicators from three categories: currency risk, sovereign debt risk and banking risk.  
† May 2008; \*\* June 2008; †† January 2008; § February 2008; # March 2008  
Source: Economist Intelligence Unit

PS: Scores are not linear

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## How to measure country risk: 3 - Market data

- Bond default spread
  - Treasury bond of emergent country - Treasury bond of stable country
- Credit Default Swap Spreads
  - A credit default swap (CDS) is a financial swap agreement that the seller of the CDS will compensate the buyer in the event of a loan default or other credit event.
- Relative volatility of markets
  - volatilidade of emergent country / volatilidade of stable country

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## Risk premium based on “Bond Default Spread”

Equity risk premium = Equity risk premium in USA + Emergent country risk premium  
(4,79%) ( ? )

$$CRP = CDS \frac{\sigma_e}{\sigma_T}$$

CRP= Country Risk Premium  
CDS = Country Default Spread  
= Treasury Yield of Emergent Country – USA Treasury Yield  
 $\sigma_e$  = Standard deviation of shares  
 $\sigma_T$  = Standard deviation of Treasury Bonds

**India Example from Damodaran, The Dark Side of Valuation, p. 68:**

$$CRP = 3\% \times \frac{31,82\%}{14,90\%} = 6,43\%$$

$$ERP = ERP_{USA} + CRP_{Emergent} = 4,79\% + 6,43\% = 11,22\%$$

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## Equity risk premium based on “relative volatility of markets”

$$ERP_{Emergent} = ERP_{USA} \frac{\sigma_{Emergent}}{\sigma_{USA}}$$

$ERP_{Emergent}$  = Equity risk premium of emergent market  
 $ERP_{USA}$  = Equity risk premium of USA  
 $\sigma_{Emergent}$  = Standard deviation of shares in the emergent country  
 $\sigma_{USA}$  = Standard deviation of shares in USA or equivalent country

**Brasil example:**

$$ERP_{Brasil} = 4,79\% \times \frac{25,83\%}{15,27\%} = 8,1\%$$

$$CRP = 8,1\% - 4,79\% = 3,31\%$$

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## Betas

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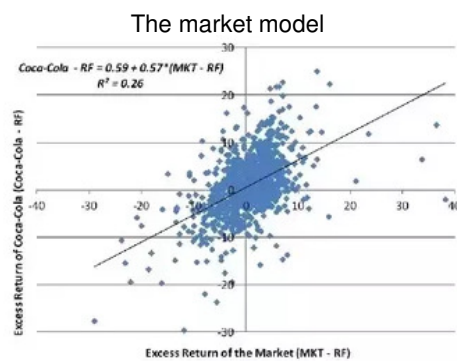
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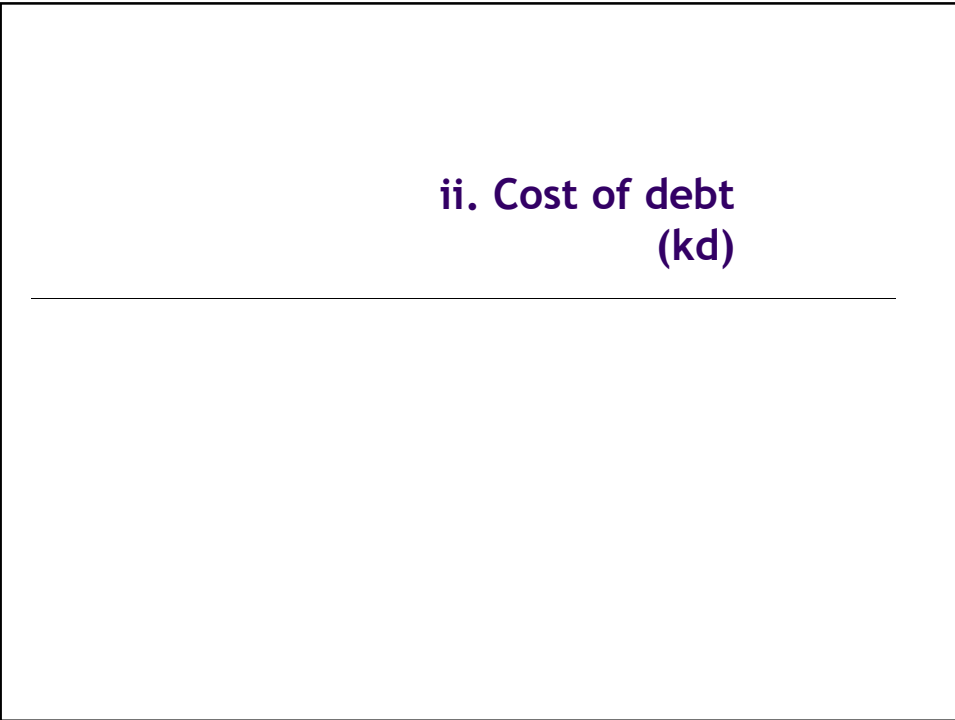
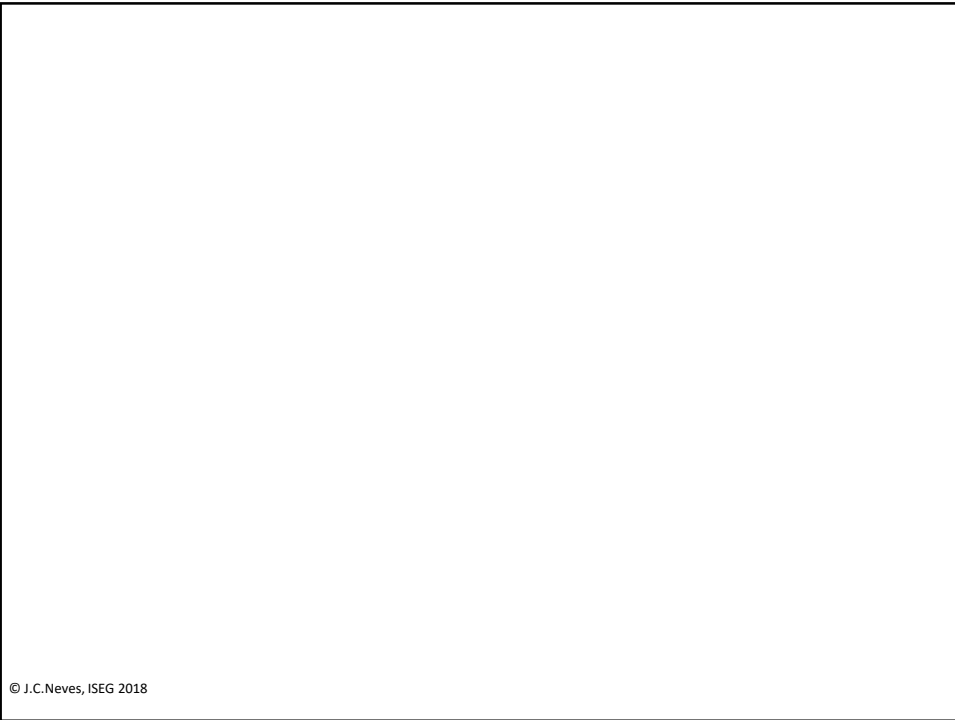
$$r_e - r_f = \alpha + \beta(r_m - r_f)$$

CAPM

The market model  
Bloomberg, Datastream, Reuters, etc.



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## Cost of debt Ranked by best practice

- The company has bonds quoted:
  - Use the yield to maturity
- The company has a rating but no bond is quoted:
  - Use yield to maturity of identical risk bonds
- No bonds are quoted and no rating:
  - Interest rate of next loan
  - Interest rate of most recent loan
  - Estimate a synthetic rating base on Times interest earning
  - Average cost of debt

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## Reuters corporate default spreads

Rating	1 yr	2 yr	3 yr	5 yr	7 yr	10 yr	30 yr
Aaa/AAA	14	16	27	40	56	68	90
Aa1/AA+	22	30	31	48	64	77	99
Aa2/AA	24	37	39	54	67	80	103
Aa3/AA-	25	39	40	58	71	81	109
A1/A+	43	48	52	65	79	93	117
A2/A	46	51	54	67	81	95	121
A3/A-	50	54	57	72	84	98	124
Baa1/BBB+	62	72	80	92	121	141	170
Baa2/BBB	65	80	88	97	128	151	177
Baa3/BBB-	72	85	90	102	134	159	183
Ba1/BB+	185	195	205	215	235	255	275
Ba2/BB	195	205	215	225	245	265	285
Ba3/BB-	205	215	225	235	255	275	295
B1/B+	265	275	285	315	355	395	445
B2/B	275	285	295	325	365	405	455
B3/B-	285	295	305	335	375	415	465
Caa/CCC+	450	460	470	495	505	515	545
US Treasury Yield	4.74	4.71	4.68	4.63	4.60	4.59	4.56

Spread values represent basis points (bps) over a US Treasury security of the same maturity, or the closest matching maturity.

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## Rating and interest coverage ratio

For smaller non-financial service companies  
(market cap < \$ 5 billion)

<i>If interest coverage ratio is</i>			
<b>greater than</b>	<b>≤ to</b>	<b>Rating is</b>	<b>Spread is</b>
12.5	100000	Aaa/AAA	0.75%
9.5	12.499999	Aa2/AA	1.00%
7.5	9.499999	A1/A+	1.10%
6	7.499999	A2/A	1.25%
4.5	5.999999	A3/A-	1.75%
4	4.499999	Baa2/BBB	2.25%
3.5	3.999999	Ba1/BB+	3.25%
3	3.499999	Ba2/BB	4.25%
2.5	2.999999	B1/B+	5.50%
2	2.499999	B2/B	6.50%
1.5	1.999999	B3/B-	7.50%
1.25	1.499999	Caa/CCC	9.00%
0.8	1.249999	Ca2/CC	12.00%
0.5	0.799999	C2/C	16.00%
-100000	0.499999	D2/D	20.00%

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Source: Damodaran, 2016

## iii. Cost of preferred equity (kp)

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## Cost of preferred shares

- No growth of dividends:
  - = dividends/Price
- Constant growth of dividends:
  - = (Dividends/Price) + g
- If there are special rights
  - Use the options theory

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## Hibrid securities

- Decompose the security into equity and debt

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## Flotation costs

- Flotation cost as a fixed cost per share

$$k_e = \frac{D_1}{P_0 - F} + g$$

- Flotation cost as a percentage of the share price

$$k_e = \frac{D_1}{P_0 \times (1 - f)} + g$$

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## iv. Weighed average cost of capital (km)

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## Weighted average cost of capital (km)

$$k_m = k_c \frac{E}{C} + k_p \frac{E_p}{C} + k_d \frac{D}{C} (1-t)$$

$$k_m = k_u \cdot \left(1 - t \frac{D}{C}\right)$$

E – Equity based on ordinary shares  
E<sub>p</sub> – Equity based on preferred shares  
D – Debt  
C = Invested Capital = E+E<sub>p</sub>+D  
t = Tax rate

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## Target capital structure is recommended to estimate WACC.

- If you do not know what is the target capital structure, then you may:
  - Read statements by management to infer what is the target capital structure
  - Assume the current capital structure as the target capital structure
  - Examine trends in the company capital structure to infer about the target capital structure
  - Use averages of comparable companies' capital structure as the target capital structure

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## v. Unlevered cost of capital ( $k_u$ )

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### Unlevered cost of capital ( $k_u$ )

- CAPM

$$k_u = r_f + \beta_u (r_m - r_f)$$

- MODIGLIANI & MILLER

$$k_u = \frac{k_m}{1 - t \times \frac{D}{D + E}}$$

Hamada Formula:

$$\beta_u = \frac{\beta_e + \beta_D \left(\frac{D}{E}\right)}{1 + \frac{D}{E}(1-t)}$$

Hamada Formula Simplified:

$$\beta_u = \frac{\beta_E}{1 + \frac{D}{E}(1-t)}$$

$$k_u = \frac{k_e + \frac{D}{E} k_d (1-t)}{1 + \frac{D}{E}(1-t)}$$

## Estimating a Beta of an unquoted company using the pure-play model

**Step 1: Select the comparable** Determine comparable company or companies. These are companies with similar business risk.



**Step 2: Estimate comparable's beta** Estimate the equity beta of the comparable company or companies.



**Step 3: Unlever the comparable's beta** Unlever the beta of the comparable company or companies, removing the financial risk component of the equity beta, leaving the business risk component of the beta.



**Step 4: Lever the beta for the project's financial risk** Lever the beta of the project by adjusting the asset beta for the financial risk of the project.

Source: Reading 36, Cost of capital, Corporate Finance, CFA level I

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## Levered betas and unlevered betas

$$\beta_E = \beta_u \left( 1 + \frac{D}{E}(1-t) \right)$$

Industry	Number of firms	Beta	Market D/E	Tax rate	Unlevered Beta
Advertising	38	1,02	69,06%	30,60%	0,69
Aerospace and Defense	27	1,02	36,89%	20,49%	0,79
Agricultural Products	33	0,82	63,38%	15,71%	0,53
...	...	...	...	...	...
Tires and Rubber	5	1,37	147,21%	32,84%	0,69
Tobacco	4	0,58	53,27%	24,63%	0,41
Trading Companies and Distributors	49	1,19	158,87%	25,88%	0,55
Trucking	16	0,93	142,43%	17,08%	0,43
Water Utilities	12	0,60	137,38%	39,13%	0,33
Wireless Telecommunication Services	11	1,00	45,26%	25,30%	0,75
<b>Grand Total</b>	<b>4167</b>	<b>1,04</b>	<b>85,33%</b>	<b>20,93%</b>	<b>0,80</b>

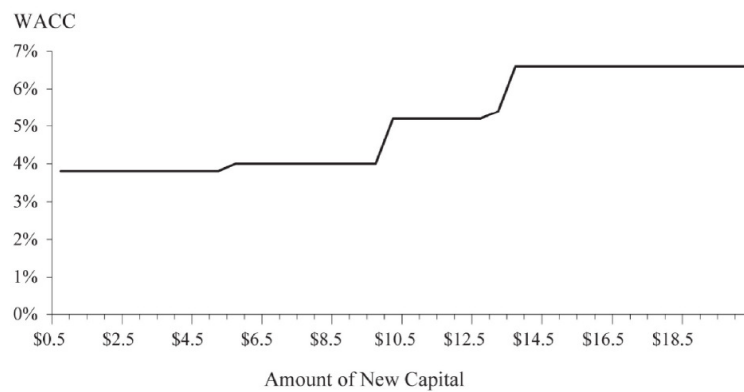
Source: <http://pages.stern.nyu.edu/~adamodar/>

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## vi. Applying the cost of capital in budgeting

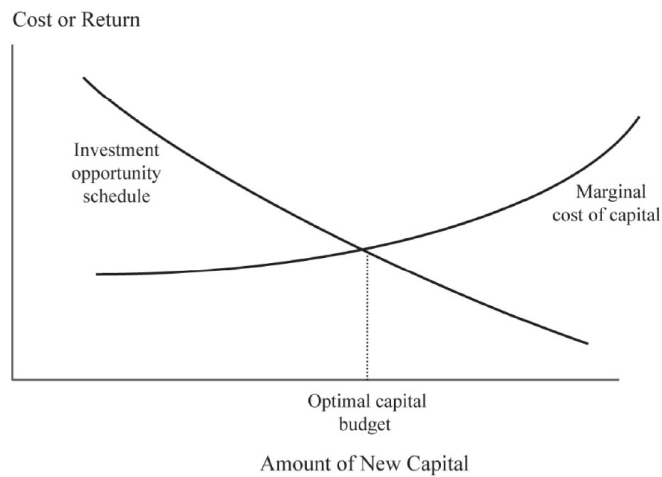
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### Marginal cost of capital schedule



Source: Reading 36, Cost of capital, Corporate Finance, CFA level I

## Optimal investment decision



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Source: Reading 36, Cost of capital, Corporate Finance, CFA level I

## What do CFO's do?

- The most popular method for estimating the cost of equity is the capital asset pricing model.
- Few companies use the dividend cash flow model to estimate a cost of equity.
- Publicly traded companies are more likely to use the capital asset pricing model than are private companies.
- In evaluating projects, the majority use a single company cost of capital, but a large portion apply some type of risk adjustment for individual projects.

Source: Reading 36, Cost of capital, Corporate Finance, CFA level I

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